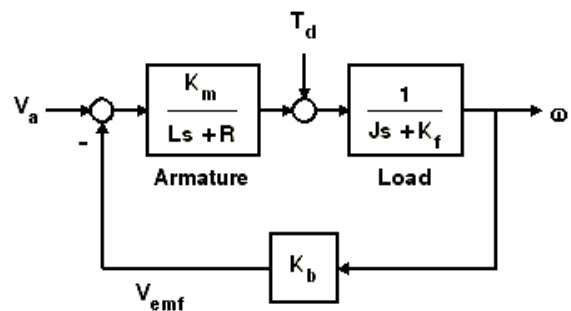
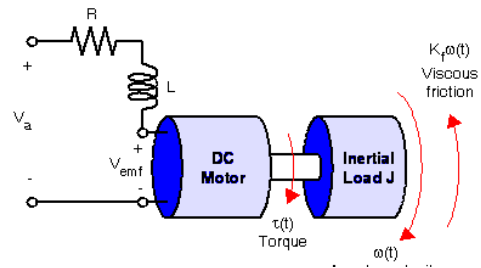


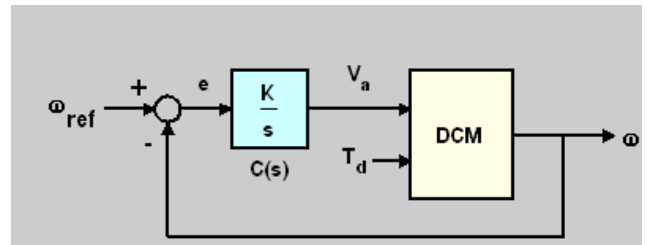
Q1.A.(60 M.) A simplified circuit and block diagram of an armature controlled dc motor is shown below.

Answer the following questions:

1. Derive a mathematical model in the form of Transfer Function.
2. Check stability of the system.
3. Find the time domain response if the system is subjected to a step input in the applied voltage, calculate all time domain specifications.
4. Find state space model
5. Find $\omega(t)$ if $\omega(0)=0.1$, neglect all other initial conditions.
6. Find the eigenvalues, comment.
7. If an integral control is inserted to the system (see the figure),
8. use root-locus technique to show the effect of the modification to the stability.
9. Find the value of K for the damping ratio to be 0.7.



For this example, the physical constants are:
 $R = 2.0$; $\% \text{ Ohms}$
 $L = 0.5$; $\% \text{ Henrys}$
 $K_m = K_b = 0.1$; $\% \text{ torque and back emf constants}$
 $K_f = 0.2$; $\% \text{ Nms}$
 $J = 0.02$; $\% \text{ kg.m}^2/\text{s}^2$



Q2.(40 M.) A mathematical model for a system is given by the following matrices (MATLAB Syntax):

$$A = [0.1 \quad 0.2; 0.3 \quad 0.4];$$

$$B = [1 \quad 0]^T;$$

$$C = [0 \quad 1];$$

$$D = [0];$$

1. Convert the model into transfer matrix form
2. Check the stability of the system
3. Calculate damping ratio, maximum overshoot and damping natural frequency.
4. Find $x(t)$, $x_0(t) = [0.1 \quad 0]$